## Hypothesis Tests for a Mean

## Stat 145

You may have noticed that although we have created confidence intervals for a mean, we have not done hypothesis tests for a mean – until now.

Remember that a randomization distribution should simulate a situation that

- reflects the design of our study and our sample data, and
- forces the null hypothesis to be true.

The randomization distributions we have seen so far have either used

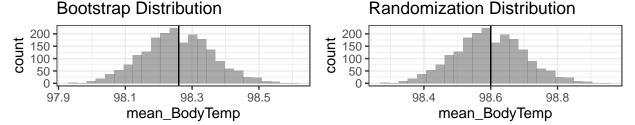
- rflip() to simulate categorical data with a specified proportion, or
- shuffle() to ensure that there is no association between two variables.

Neither of these will work for a hypothesis about a mean. We need a new idea. Here it is:

We can create a randomization distribution for a test about a single mean by shifting the bootstrap distribution to make it centered in the right location.

This will give us a distribution that is centered at the value specified by the null hypothesis and the appropriate amount of variability. Here's how.

```
mean(~BodyTemp, data = BodyTemp50)
## [1] 98.26
# Create the Bootstrap distribution
Temp_boot <-
    do(2000) * df_stats( ~ BodyTemp, data = resample(BodyTemp50), mean_BodyTemp = mean)
# Shift it so that it is centered in the correct place for our hypothesis
Temp_null <-
    Temp_boot %>% mutate(mean_BodyTemp = mean_BodyTemp + (98.6 - 98.26))
```



Notice that 98.6 lies outside the 95% confidence interval and the p-value is than 0.05.

```
# 95% confidence interval
cdata(~ mean_BodyTemp, data = Temp_boot)
## lower upper central.p
## 2.5% 98.05 98.47 0.95
# p-value for test of HO: mu = 98.6
2 * prop(~ (mean_BodyTemp <= 98.26), data = Temp_null)</pre>
```

## prop\_TRUE ## 0