

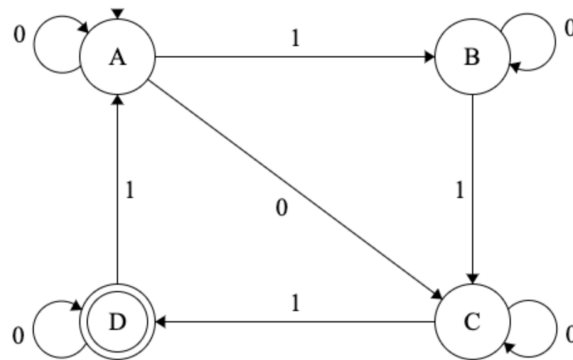
### 3.6 The Equivalence of DFA and NFA.

Despite their apparent differences, DFAs and NFAs recognize exactly the same set of languages. That is

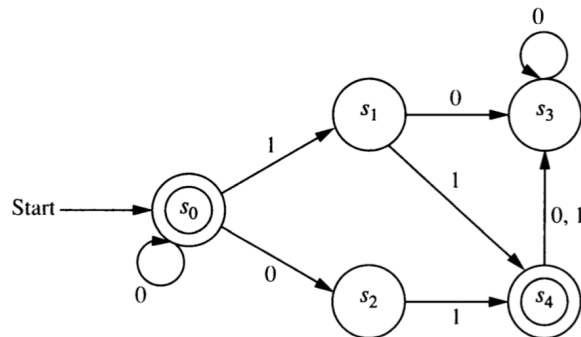
- If the language  $L$  is recognized by a DFA  $M$ , then there is also an NFA  $N$  that recognizes  $L$ .
- If the language  $L$  is recognized by an NFA  $N$ , then there is also a DFA  $M$  that recognizes  $L$ .

To prove this, we need

- Algorithm 1: an algorithm that converts DFAs into equivalent NFAs
  - Algorithm 2: an algorithm that converts NFAs into equivalent DFAs.
20. One of these two algorithms is super easy. Which one? What is the algorithm?
21. The other direction is more interesting. Let's see if we can figure out a general algorithm for this task by first exploring an example. Consider the following NFA. Create an equivalent DFA, using a method that could be applied to any NFA.



22. Now convert the NFA  $N_1$  into an equivalent DFA. Here's  $N_1$  again.



23. If an NFA has  $n$  states and we use this method to convert it to a DFA, what is the most states the DFA might have?